

Optimize & Fit

Find minima, roots, and best-fit parameters. from scipy.optimize import ...

PURPOSE	COMMAND	RESULT
Minimize a scalar function.	<code>minimize(f, x0=[0,0], method="BFGS")</code>	
Solve $f(x) = 0$ in a bracket.	<code>root_scalar(f, bracket=[0,2], method="brentq")</code>	
Solve a nonlinear system.	<code>root(fun, x0=[0, 0])</code>	
Fit a model curve to data.	<code>curve_fit(model, xdata, ydata, p0=[1,1,0])</code>	
Nonlinear least squares.	<code>least_squares(resid, x0=[0, 0])</code>	
Solve a linear program.	<code>linprog(c, A_ub, b_ub, bounds=...)</code>	

every solver returns an OptimizeResult; check res.success before trusting res.x

Linear Algebra

Solve systems, decompose matrices, and measure them. from scipy import linalg

PURPOSE	COMMAND	RESULT
Solve $Ax = b$.	<code>linalg.solve(A, b)</code>	
LU decomposition.	<code>linalg.lu(A)</code>	
Eigenvalues / vectors.	<code>linalg.eig(A)</code>	
Singular value decomp.	<code>linalg.svd(A)</code>	
Cholesky factor (SPD).	<code>linalg.cholesky(A, lower=True)</code>	
Determinant, inverse, norm.	<code>linalg.det / .inv / .norm</code>	

never invert to solve a system: call solve(A, b); decompose for structure

Integrate & ODEs







Numerically integrate functions, samples, and differential equations.

PURPOSE	COMMAND	RESULT
Definite integral of a function.	<code>quad(f, 0, np.inf)</code>	
Double integral over a region.	<code>dblquad(f, 0, 1, 0, 1)</code>	
Integrate samples (trapezoid).	<code>trapezoid(y, x)</code>	
Integrate samples (Simpson).	<code>simpson(y, x=x)</code>	
Solve an initial-value ODE.	<code>solve_ivp(f, [0, 10], y0=[2.0])</code>	

quad integrates a callable; trapezoid/simpson integrate samples you already have

Interpolate

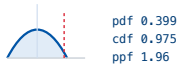





Build a callable that fills in values between your data points.

PURPOSE	COMMAND	RESULT
1-D cubic spline through points.	<code>CubicSpline(x, y)</code>	
Generic 1-D interpolation.	<code>interp1d(x, y, kind="cubic")</code>	
Shape-preserving (monotone).	<code>PchipInterpolator(x, y)</code>	
Smoothing B-spline fit.	<code>make_splrep(x, y, s=0.5)</code>	
Scattered 2-D interpolation.	<code>griddata(points, values, xi)</code>	
Smooth scattered N-D (RBF).	<code>RBFInterpolator(points, values)</code>	

interpolation turns discrete (x, y) samples into a callable you evaluate anywhere

Statistics






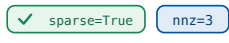
Distributions, summaries, and hypothesis tests via `scipy.stats`.

PURPOSE	COMMAND	RESULT
Distribution pdf / cdf / ppf.	<code>norm.pdf(0) .cdf(1.96) .ppf(.975)</code>	
Freeze a distribution.	<code>dist =norm(loc=10, scale=2)</code>	
Two-sample t-test.	<code>ttest_ind(a, b)</code>	
Correlation between vectors.	<code>pearsonr(x, y)</code>	
Simple linear regression.	<code>linregress(x, y)</code>	
Bootstrap a confidence interval.	<code>bootstrap((data,), np.mean)</code>	

read tests off the result's `.statistic` and `.pvalue`; freeze a dist and reuse it

Sparse Matrices

Store and solve with mostly-zero matrices using the modern array API.

PURPOSE	COMMAND	RESULT
Build from coordinates (COO).	<code>coo_array((data, (row, col)), shape=(3,3))</code>	
Convert to CSR for math.	<code>A = A.tocsr()</code>	
Sparse identity / diagonals.	<code>eye_array(3)diags_array(...)</code>	
Densify to a NumPy array.	<code>A.toarray()</code>	
Solve a sparse linear system.	<code>spsolve(A.tocsc(), b)</code>	
Check sparsity / nonzeros.	<code>issparse(A) A.nnz</code>	

prefer the sparse `*array*` classes; build in COO, convert to CSR/CSC, `toarray()` last

Signal & FFT


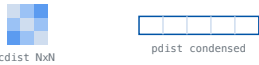


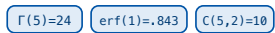

Filter, transform, and find structure in 1-D signals.

PURPOSE	COMMAND	RESULT
Design a Butterworth filter.	<code>butter(4, 0.2, btype="low")</code>	
Zero-phase filtering.	<code>filtfilt(b, a, x)</code>	
Fast Fourier transform.	<code>fft.fft(x) fft.fftfreq(n, d)</code>	
Power spectral density.	<code>periodogram(x, fs=500)</code>	
Find peaks in a signal.	<code>find_peaks(x, height=0.5)</code>	
Convolve two sequences.	<code>convolve(a, v)</code>	

design (butter) -> apply without distorting timing (filtfilt) -> inspect (fft)

Spatial & Special

Nearest-neighbor queries, geometry, and the special functions library.

PURPOSE	COMMAND	RESULT
KD-tree, query neighbors.	<code>KDTree(pts).query(q, k=1)</code>	
Pairwise distance matrices.	<code>distance.cdist(A, B) .pdist(A)</code>	
Convex hull of points.	<code>ConvexHull(pts)</code>	
Delaunay triangulation.	<code>DeLaunay(pts)</code>	
Special functions.	<code>special.gamma / .erf / .comb</code>	
ML helpers (expit, softmax).	<code>special.expit / .softmax</code>	

scipy.spatial answers geometry; scipy.special catalogs math + stable ML helpers